

Peter Botschwina

On the equilibrium structures and the IR active bending vibrations of linear C₁₃ and C₁₅: results of large-scale coupled cluster calculations

Received: 15 July 2005 / Accepted: 19 July 2005 / Published online: 23 September 2005
© Springer-Verlag 2005

Abstract Accurate equilibrium (r_e) structures (ca. 0.0005 Å accuracy in bond lengths) have been established for linear C₁₃ and C₁₅ by applying a uniform correction to the results of CCSD(T) calculations with the cc-pVQZ basis set. The equilibrium bond lengths cover a small range between 1.2690 and 1.2928 Å and are indicative of strong carbon–carbon double bonds. Equilibrium structures of still longer chains may be obtained by taking the recommended r_e structure for C₁₅ and inserting one or more C₂ links with $R_e = 1.277$ Å in the middle of the molecule. Both linear C₁₃ and C₁₅ exhibit no sign of floppiness and appear to behave like fairly normal semi-rigid molecules. Diagonal potentials for the IR active bending vibrations of both molecules have large correlation contributions between -33 and 47%, with MP2 strongly overshooting with respect to CCSD(T). Harmonic *cis*-bending vibrational wavenumbers and their absolute IR intensities are predicted. Since the latter are rather small, the chances of an interstellar detection of linear C₁₃ or C₁₅ in the far IR may be poor.

Keywords Carbon chains · Coupled cluster · Equilibrium structures · Bending vibrations · IR intensities

1 Introduction

Linear carbon chains are of considerable interest to the chemistry of combustion and astrochemistry (see [1, 2] for reviews). Since they have no permanent electric dipole moment, radio astronomy does not provide the appropriate technique to observe such species in the interstellar medium (ISM) or the circumstellar medium (CSM). However, astronomical observations of the first members of pure carbon chains in the

infrared (IR) and visible region of the spectrum have been successful. C₃, which has a linear equilibrium structure and a very shallow bending potential (see, e.g., [3]), has been observed in the circumstellar envelope of the evolved carbon star IRC+10216 through its antisymmetric stretching vibration (ν_3) [4]. Through its bending vibrational transition (ν_2) in the far infrared (FIR) region at ca. 65 cm⁻¹, C₃ was found in the same astronomical source as well as in the direction of Sagittarius B2, making use of either the Infrared Space [5] or the Kuiper Airborne Observatory [6]. Rovibronic transitions of C₃ near 4050 Å have been known to astronomers since its detection in cometary tails as early as in 1881 [7]. The molecule was also observed in the same wavelength region in the atmosphere of cool stars (see [8] for a review) and even in the diffuse ISM [9, 10]. While the interstellar detection of linear C₄ must be considered to be tentative [11], linear C₅ was definitely observed in IRC+10216 through its antisymmetric stretching vibration of highest wavenumber, termed ν_3 [12].

There is an ongoing debate whether longer carbon chains will have bending vibrational transitions with sufficiently large intensities such that satellite-based observation of spectra in the FIR might be possible. It is a major goal of this paper to address this question. Linear C₁₃ and C₁₅ have been selected for this purpose. For the former species, high-resolution mid-IR spectra have been published [13, 14]. However, no reliable gas-phase spectroscopic information is yet available for the bending vibrations of either linear C₁₃ or C₁₅.

Previous quantum-chemical studies of spectroscopic properties for linear C₁₃ are of rather unknown reliability, in particular with respect to the calculated wavenumbers and intensities of the IR active bending vibrations. In 1994, SCF calculations with the small 6–31G* basis set were published by Bleil et al. [15]. The results of SCF, CASSCF (8/8) and DFT/B3LYP calculations for harmonic vibrational wavenumbers and IR intensities as obtained within the double harmonic (DH) approximation were reported by Martin and Taylor [16] and Martin et al. [17]. Dunning's cc-pVDZ basis [18], which comprises 182 contracted Gaussian-type orbitals (cGTOs), was employed in these calculations.

Dedicated to Prof. Dr. H. Stoll on the occasion of his 60th birthday.

P. Botschwina
Institut für Physikalische Chemie, Universität Göttingen,
Tammannstraße 6, 37077 Göttingen, Germany
Tel.: +49-551-393133, Fax: +49-551-393144,
E-mail: pbotsch@gwdg.de

Table 1 Parameters (in a.u.) of near-equilibrium *cis*-bending potential energy functions for linear C₁₃^a

Term	SCF vqz	MP2 vqz	CCSD vqz	CCSD(T) vqz	CCSD(T) vtz
S ₁ ²	0.011639	0.024119	0.013343	0.015355	0.016796
S ₁ ⁴	-0.000537	-0.001515	-0.000553	-0.000139	-0.002897
S ₂ ²	0.072830	0.044373	0.057690	0.050543	0.052885
S ₂ ⁴	0.001088	-0.000391	0.000750	0.000471	-0.004609
S ₃ ²	0.016458	0.034133	0.020326	0.024128	0.025725
S ₃ ⁴	-0.000420	-0.001551	-0.000137	-0.000285	-0.003651
S ₄ ²	0.069989	0.039075	0.054573	0.047221	0.048299
S ₄ ⁴	0.000017	-0.001644	0.000075	-0.000139	-0.002105
S ₅ ²	0.017519	0.035665	0.021050	0.024752	0.025926
S ₅ ⁴	-0.001689	-0.003627	-0.001581	-0.001718	-0.003523
S ₆ ²	0.068848	0.037413	0.053423	0.046053	0.047114
S ₆ ⁴	0.001922	0.000134	0.002380	0.002263	-0.001959
S ₁ S ₂	0.005557	0.001609	0.002232	0.001922	0.001393
S ₁ S ₃	-0.001231	-0.002150	-0.001444	-0.001453	-0.002083
S ₁ S ₄	-0.000330	-0.000082	-0.000066	0.000042	0.000094
S ₁ S ₅	-0.000064	-0.000066	-0.000033	0.000009	-0.000066
S ₁ S ₆	-0.000028	-0.000104	-0.000058	-0.000067	-0.000005
S ₂ S ₃	0.014234	0.013739	0.013230	0.013768	0.014107
S ₂ S ₄	-0.008032	-0.005893	-0.007091	-0.006157	-0.006232
S ₂ S ₅	-0.001155	-0.001149	-0.001083	-0.001002	-0.001658
S ₂ S ₆	0.000671	0.000395	0.000592	0.000568	0.000486
S ₃ S ₄	0.011780	0.011473	0.011063	0.011909	0.011918
S ₃ S ₅	-0.001459	-0.002971	-0.001953	-0.002079	-0.002494
S ₃ S ₆	-0.001297	-0.001486	-0.001335	-0.001261	-0.001579
S ₄ S ₅	0.012778	0.012425	0.011949	0.012733	0.012922
S ₄ S ₆	-0.011335	-0.007730	-0.009796	-0.008285	-0.008645
S ₅ S ₆	0.018375	0.018280	0.017398	0.018597	0.018824

^aSee Eq. (1a–2) for the definition of symmetry coordinates and PEF terms. All calculations are carried out around the CCSD(T)/cc-pVQZ equilibrium structure

2 Details of calculations and results

Like in the author's previous work on closed-shell carbon chains [19–22], the coupled cluster variant CCSD(T) [23] is employed as the most sophisticated ab initio method of the present study. For comparison, various results obtained by HF-SCF, MP2 and CCSD will be quoted as well. Most of the present calculations make use of Dunning's cc-pVQZ basis set [18], which involves 55 cGTOs per carbon atom. Such calculations for C₁₃ and C₁₅ thus comprise 715 and 825 cGTOs, respectively. As has been shown earlier for C₃ [3], a basis set of this size may be mandatory to obtain accurate results for shallow CCC bending potentials. Throughout, valence electrons are correlated in the post-Hartree-Fock calculations. All electronic structure calculations of the present work were carried out with the MOLPRO suite of programmes [24–26].

Calculated equilibrium structures for linear C₁₃ and C₁₅ as obtained by the four different ab initio methods noted above are displayed in Fig. 1. The figure also includes recommended equilibrium bond lengths which were derived from the CCSD(T) values by subtracting a uniform correction of 0.0037 Å as established earlier (see [22] and references therein). It mainly corrects for the neglect of core–valence and core–core correlation, but should also account for smaller

errors arising from basis set incompleteness and the approximations made in CCSD(T), i.e., neglect of connected quadruple and higher substitutions and non-iterative treatment of connected triples. The resulting recommended equilibrium (*r_e*) structure for C₁₃ agrees closely (maximum difference: 0.0006 Å) with the author's previous work [22], which involved CCSD(T) calculations with the smaller cc-pVTZ basis set [18]. The equilibrium rotational constant as obtained from the recommended *r_e* structure of the present work is B_e=141.66 MHz, to be compared with the author's previous value of 141.69 MHz [22] and the experimental ground-state rotational constant of B₀=141.87(2) MHz [13], where the standard deviation in terms of the least significant digit is given in parentheses.

The lower part of Fig. 1 summarizes the results obtained for linear C₁₅. Upon comparison with those calculated for C₁₃, no great differences are observed. Again, as emphasized in the author's previous work on linear C₁₁ [22], connected triple substitutions provide non-negligible and non-uniform contributions to the individual carbon–carbon equilibrium bond lengths. Like for C₁₃ and C₁₁, the MP2 results are surprisingly close to those obtained by CCSD(T), the maximum deviation not exceeding 0.0033 Å. However, this must be considered to be a result of fortuitous error cancellation since

Table 2 Diagonal part of *cis*-bending potential energy functions for linear C₁₅^a

Term	SCF vqz	MP2 vqz	CCSD vqz	CCSD(T) vqz	CCSD(T) vtz
S ₁ ²	0.011885	0.024594	0.013601	0.015608	0.017145
S ₁ ⁴	-0.000687	-0.001167	-0.000600	-0.000145	-0.003173
S ₂ ²	0.072641	0.043681	0.057438	0.050239	0.052717
S ₂ ⁴	0.001025	-0.000097	0.000740	0.000603	-0.004957
S ₃ ²	0.016765	0.035128	0.020703	0.024503	0.026068
S ₃ ⁴	-0.000456	-0.001710	-0.000327	-0.000370	-0.003027
S ₄ ²	0.069293	0.037528	0.053784	0.046380	0.047593
S ₄ ⁴	0.000396	-0.001110	0.000575	0.000456	-0.002231
S ₅ ²	0.018769	0.038736	0.022605	0.026399	0.027818
S ₅ ⁴	-0.001231	-0.002093	-0.000514	-0.000453	-0.004209
S ₆ ²	0.063944	0.032536	0.048967	0.042111	0.043167
S ₆ ⁴	-0.002718	-0.003847	-0.002371	-0.001946	-0.003353
S ₇ ²	0.019436	0.040001	0.023272	0.027004	0.028038
S ₇ ⁴	-0.000840	-0.002423	0.000261	0.000427	-0.003708

^aSee Eq. (1a–2) for the definition of symmetry coordinates and PEF terms. All calculations are carried out around the CCSD(T)/cc-pVQZ equilibrium structure. All values in a.u.

							C ₁₃ X ¹ Σ _g ⁺							
							1.2590	1.2823	1.2507	1.2690	1.2571	1.2629	HF-SCF	
							1.2951	1.2943	1.2747	1.2828	1.2783	1.2804	MP2	
							1.2789	1.2905	1.2644	1.2782	1.2695	1.2737	CCSD	
							1.2923	1.2956	1.2731	1.2837	1.2773	1.2804	CCSD(T)	
C	=	C	=	C	=	C	=	C	=	C	=	C	...	
1.2886		1.2919		1.2694		1.2800		1.2736		1.2767				recommended
														C ₁₅ X ¹ Σ _g ⁺
							1.2581	1.2840	1.2492	1.2712	1.2550	1.2656	1.2604	HF-SCF
							1.2953	1.2949	1.2748	1.2833	1.2783	1.2812	1.2800	MP2
							1.2783	1.2917	1.2635	1.2798	1.2682	1.2754	1.2721	CCSD
							1.2920	1.2965	1.2727	1.2848	1.2766	1.2819	1.2794	CCSD(T)
C	=	C	=	C	=	C	=	C	=	C	=	C	...	
1.2883		1.2928		1.2690		1.2811		1.2729		1.2782		1.2757		recommended

Fig. 1 Ab initio (basis set: cc-pVQZ) and recommended equilibrium bond lengths (in Å) for linear C₁₃ and C₁₅

MP2 takes only double substitutions explicitly into account. From the recommended *r_e* structure, B_e(C₁₅) = 92.11 MHz is obtained. The corresponding ground-state value is predicted as B₀ = 92.2(1) MHz, where the estimated error in terms of the least significant digit is given in parentheses.

Figure 2 graphically displays the recommended equilibrium bond lengths for linear C₁₅ in an analogous way as done earlier for linear C₁₄ [22]. Again, oscillatory behavior is observed and the innermost CC equilibrium bond lengths are approaching a constant value of 1.277 Å. An almost identical value of 1.276 Å was obtained for the C_{2_n} series with ³∑_g⁻ ground states [22]. We may therefore predict equilibrium structures of still larger carbon chains of type C_{2_n+1} with reasonable accuracy by starting with the recommended *r_e* structure for C₁₅ and inserting one or more C₂ links with R_e = 1.277 Å in the middle of the molecule. B_e predictions for linear C₁₇ and C₁₉ obtained in this way are 63.23 and 45.27 MHz, respectively. The corresponding B₀ values are expected to be only slightly larger.

In order to describe the IR active bending vibrations of C_{2_n+1} chains, which are of π_u symmetry and lead to *cis*-like distortions of the nuclear framework out of the equilibrium structure of D_{∞h} symmetry, we make use of normalized symmetry coordinates. They are defined as

$$S_i = \frac{1}{\sqrt{2}} (\Delta\alpha_i + \Delta\alpha'_i) \quad i = 1, 2, \dots, n-1 \quad (1a)$$

$$S_n = \Delta\beta \quad (\beta : \text{central CCC angle}) \quad (1b)$$

The integer *n* may also be interpreted as the number of pairwise equivalent bonds. In the present work, these are counted from outermost to innermost and the angular symmetry coordinates accordingly. Near-equilibrium analytical potential energy functions (PEFs) for the *cis*-bending vibrations of linear C₁₃ and C₁₅ are obtained from ab initio calculations around the CCSD(T)/cc-pVQZ equilibrium structures using distortions of 1°, 5° and 10° for diagonal cuts and additionally pairwise (1°, 1°) distortions in order to determine the quadratic coupling terms. The resulting analytical PEFs as obtained by

Table 3 CCSD(T)/cc-pVTZ quadratic coupling terms (in a.u.) for linear C₁₅^a

Term	Value (a.u.)	Term	Value (a.u.)
S ₁ S ₂	0.001301	S ₃ S ₄	0.011769
S ₁ S ₃	-0.002132	S ₃ S ₅	-0.002367
S ₁ S ₄	0.000069	S ₃ S ₆	-0.001293
S ₁ S ₅	0.000049	S ₃ S ₇	-0.000164
S ₁ S ₆	-0.000056	S ₄ S ₅	0.014337
S ₁ S ₇	-0.000100	S ₄ S ₆	-0.005770
S ₂ S ₃	0.014358	S ₄ S ₇	-0.001889
S ₂ S ₄	-0.006087	S ₅ S ₆	0.011647
S ₂ S ₅	-0.001914	S ₅ S ₇	-0.003618
S ₂ S ₆	0.000405	S ₆ S ₇	0.019578
S ₂ S ₇	-0.000106		

^a See Eq. (1a–2) for the definition of symmetry coordinates and PEF terms. Calculations are carried out around the CCSD(T)/cc-pVQZ equilibrium structure

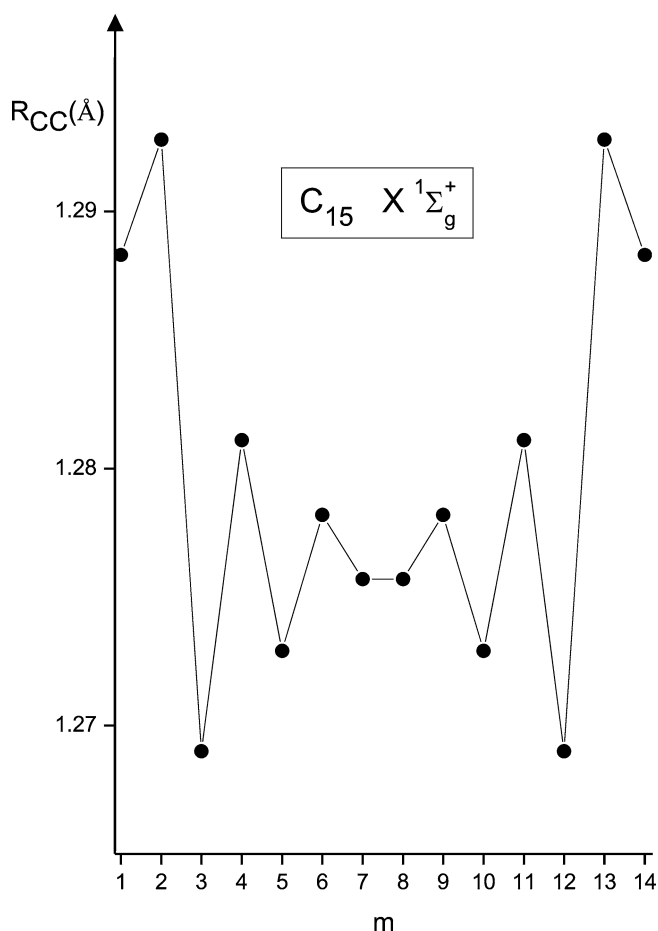


Fig. 2 Comparison of recommended equilibrium bond lengths for linear C₁₅. The index *m* counts the CC bonds, starting with the outermost bond

least-squares fitting have the form

$$V - V_{\text{ref}} = \sum_{i=1}^n (C_i^{(2)} S_i^2 + C_i^{(4)} S_i^4) + \sum_{i<j}^n C_{ij} S_i S_j \quad (2)$$

The PEF parameters calculated for linear C₁₃ are listed in Table 1. The diagonal PEF part is dominated by the quadratic terms, with the quartic terms being rather insignificant for angular distortions of less than 10°. Electron correlation plays

an important role. At the CCSD(T)/cc-pVQZ level, the S_i^2 terms exhibit alternating correlation contributions between -33 and 47%. Connected triple substitutions also provide alternating contributions between -14 and 18%, when taken with respect to the corresponding CCSD(T) values. MP2 strongly overestimates the correlation effects on all six S_i^2 terms, most significantly for the S_1^2 , S_3^2 and S_5^2 terms which are larger than the corresponding CCSD(T) values by 57, 42 and 44%, respectively. Among the off-diagonal quadratic terms, those involving the coordinate pairs S_2S_3 , S_3S_4 , S_4S_5 and S_5S_6 play the largest role. The differences between the results obtained by the four different methods are rather small for these terms. The next most important coupling term, involving the combination S_4S_6 , shows significantly larger differences. Reduction of the basis set from cc-pVQZ to cc-pVTZ has little effect on the largest coupling terms. The maximum difference of 0.000656 a.u. occurs for the S_2S_5 term; this is only 4% of the largest coupling term (S_5S_6), however.

The parameters of the *cis*-bending PEFs calculated for linear C₁₅ are listed in Tables 2 (diagonal part) and 3 (quadratic coupling terms). For economical reasons, the coupling terms were only calculated with the smaller cc-pVTZ basis set (450 cGTOs). On the whole, the situation is quite similar to that discussed for C₁₃ and the results of the present work should be transferable to still larger carbon chains.

In previous papers from the Saykally group [2, 27, 28], the potential for bending around the central carbon atom has been considered to be a measure of the degree of floppiness of a C_{2n+1} species. While spectroscopists have no means to directly get such information, theory is in an easy position to do so. CCSD(T)/cc-pVQZ bending potential curves for bending around the central carbon atom with carbon-carbon distances fixed at their equilibrium values are displayed in Fig. 3 for linear C₁₅, C₁₃ and C₃. Like in the previous comparison of C_{2n+1} species with *n*=1–5 (cf. Fig. 2 of Ref. [20] and Fig. 2 of Ref. [29]) one clearly sees that C₃ is the exception while C₁₃ and C₁₅ have steep and almost quadratic bending potentials.

Absolute IR intensities for the *cis*-bending vibrations of linear C₁₃ and C₁₅ have been calculated within the familiar double-harmonic approximation which requires the knowledge of the harmonic vibrations and the first dipole moment

Table 4 First dipole moment derivatives (in a.u.) for linear C₁₃ and C₁₅ with respect to normalized π_u symmetry coordinates^a

	C ₁₃				C ₁₅			
	SCF	MP2	CCSD	CCSD(T)	SCF	MP2	CCSD	CCSD(T)
S ₁	-0.565	-1.161	-0.834	-0.944	-0.586	-1.177	-0.855	-0.960
S ₂	-1.696	-1.865	-1.788	-1.767	-1.747	-1.911	-1.840	-1.814
S ₃	-1.464	-2.149	-1.768	-1.835	-1.563	-2.240	-1.879	-1.939
S ₄	-2.120	-2.340	-1.986	-2.213	-2.261	-2.466	-2.403	-2.341
S ₅	-1.811	-2.533	-2.142	-2.190	-2.029	-2.756	-2.371	-2.396
S ₆	-1.612	-1.775	-1.719	-1.686	-2.545	-2.784	-2.719	-2.647
S ₇					-1.538	-2.064	-1.789	-1.801

^a Throughout, the recommended equilibrium structures (cf. Fig. 1) are taken as reference structures in the calculation of dipole moment derivatives which make use of the avtz' basis (sp(avtz) + df(vtz))

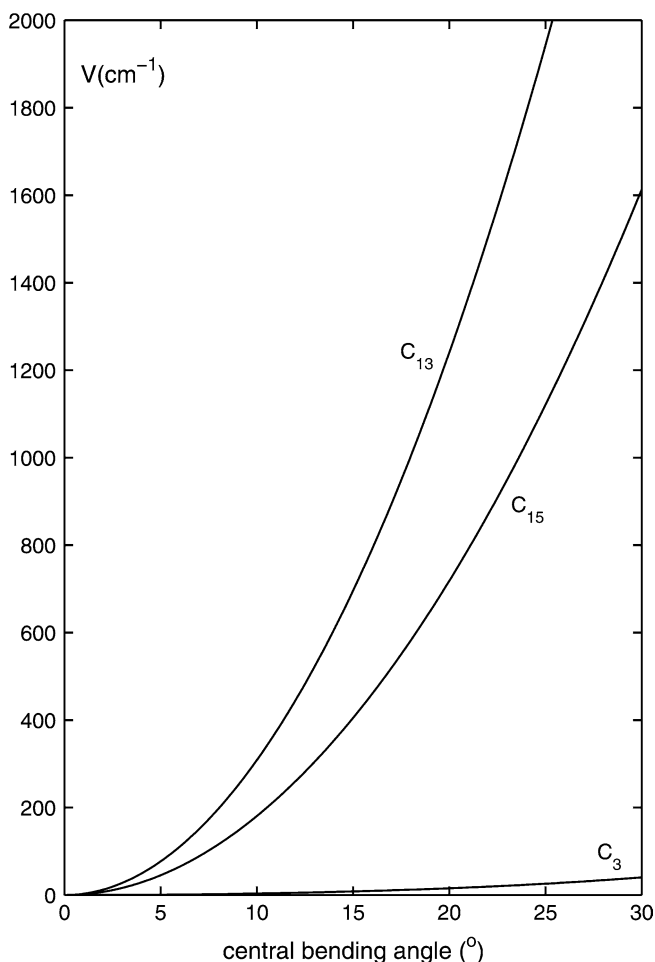


Fig. 3 Comparison of CCSD(T)/cc-pVQZ potentials of linear C₁₅, C₁₃ and C₃ for bending about the central carbon atom (bond lengths and other angles kept fixed at their equilibrium values)

derivatives. For the post-Hartree-Fock methods employed in the present work, which do not obey the Hellmann–Feynman theorem, the correlation contributions to the electric dipole moment were calculated as numerical derivatives of the correlation energies with respect to the strength of a uniform electric field, with ± 0.0001 a.u. being taken in the actual calculations. Basis sets of 442 and 510 cGTOs were employed for linear C₁₃ and C₁₅, respectively. They correspond

to extensions of Dunning's cc-pVTZ set [18] by the diffuse *s* and *p* functions from the aug-cc-pVTZ set [30].

Computed first dipole moment derivatives with respect to the *cis*-bending symmetry coordinates S_{*i*} (*i* = 1–*n*) for both carbon chains are listed in Table 4. Upon bending the terminal carbon atoms away from linearity by a given small angle produces the smallest change in the dipole moment among the *n* symmetry coordinates. The corresponding correlation contribution is as large as 67% for C₁₃ and 64% for C₁₅. Compared with CCSD(T), MP2 always overestimates the correlation contributions. For some of the symmetry coordinates, these are rather small on a percentage scale, however.

The absolute IR intensities of the *n cis*-bending vibrations were calculated according to the formula:

$$A_i = \frac{N_A g_i}{12c_0^2 \epsilon_0} \left[\sum_{j=1}^n \left(\frac{\partial \mu_{\perp}}{\partial S_j} \right)_e L_{ji} \right]^2 \quad (3)$$

In Eq. (3), N_A is Avogadro's number, c₀ the vacuum velocity of light, ϵ_0 the permittivity of vacuum and g_{*i*} the degeneracy of the vibration under study (2 in the present case). L_{*ij*} are elements of the L matrix which connects the symmetry coordinates with the normal coordinates. When the dipole moment derivatives $(\partial \mu_{\perp} / \partial S_j)_e$, the L matrix elements and the fundamental physical constants are given in atomic units, the conversion factor to A (in km mol⁻¹) is $1.777 \cdot 10^6$.

Results for the *cis*-bending vibrations of linear C₁₃ are listed in Table 5. The harmonic bending vibration with highest wavenumber, termed ω_{18} , is predicted at 508 cm⁻¹, to be compared with the author's previous CCSD(T)/cc-pVQZ values for C₅ [21] and C₇ [20] of 544.1 and 528.6 cm⁻¹, respectively. The previous calculations by Martin and Taylor [16] and Martin et al. [17] grossly overestimate ω_{18} (C₁₃). Poor agreement with the present work is also observed for ω_{19} . The harmonic wavenumbers from the present CCSD(T) calculations should be accurate to ca. 1% (cf. [21] for the quality of such calculations). Since no large anharmonicity effects are expected, they should also provide good estimates for the corresponding anharmonic values. The lowest vibrational transition of linear C₁₃ is predicted at 23 cm⁻¹, with an absolute IR intensity of 9 km mol⁻¹. Despite of the failure of the previous work for the bending vibrations with higher wavenumber, agreement among the four different calculations for the vibration with lowest wavenumber is quite good.

Table 5 Harmonic wavenumbers (in cm⁻¹) and IR intensities (in km mol⁻¹; in parentheses) for IR active bending vibrations of linear C₁₃

	SCF/vdz ^a [16]	CASSCF/vdz ^a [16]	B3LYP/vdz ^a [17]	CCSD(T) this work
ω_{18}	804(142)	793(92)	818(18)	508(14.1)
ω_{19}	656(12)	649(18)	633(0)	486(3.4)
ω_{20}	534(0)	511(0)	472(1)	426(6.6)
ω_{21}	239(4)	244(4)	263(12)	224(9.2)
ω_{22}	119(8)	124(6)	125(14)	112(14.7)
ω_{23}	25(8)	27(10)	25(8)	23(9.1)

^a Published intensities [16,17] have been multiplied by a factor of 2 in order to be consistent with the results of the present work (cf. Eq. (3))

Table 6 CCSD(T) harmonic wavenumbers and IR intensities for π_u vibrations of linear C₁₅

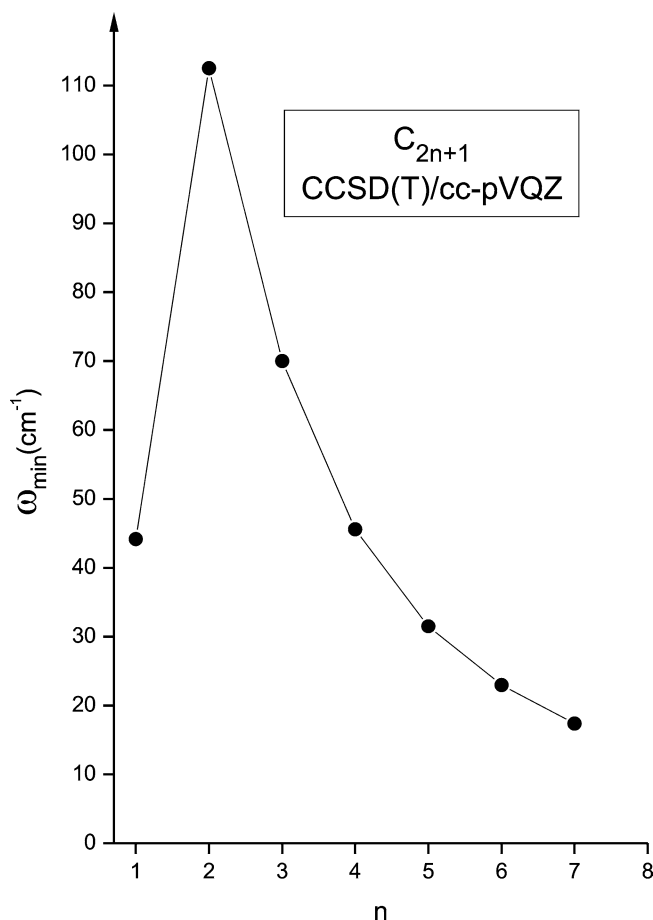
No.	ω (cm ⁻¹)	A (km mol ⁻¹)
21	506	12.6
22	483	4.2
23	453	0.0
24	281	1.9
25	188	11.3
26	88	12.5
27	17	7.6

Combining the CCSD(T)/cc-pVQZ diagonal quadratic PEF terms with the off-diagonal terms as calculated with the smaller cc-pVTZ basis set leads to changes in the harmonic wavenumbers of less than 3 cm⁻¹. In particular, the differences in the lowest two wavenumbers (ω_{22} and ω_{23}) are only 0.2 and 0.1 cm⁻¹, respectively.

CCSD(T) results for linear C₁₅ are reported in Table 6. The wavenumber of the highest *cis*-bending vibration (ω_{21}) differs from the corresponding value for C₁₃ by only 1.4 cm⁻¹. With increasing chain length, there appears to be convergence towards a lower constant value around 500 cm⁻¹, quite different from the previous calculations [16,17] which predicted an increase in that wavenumber with chain length. Throughout, the absolute intensities of the *cis*-bending vibrations are relatively small, with the largest value of 12.6 km mol⁻¹ calculated for ω_{21} . The bending vibration of lowest wavenumber (ω_{27}) is predicted at 17.4 cm⁻¹. This value is expected to provide a good approximation to the corresponding anharmonic wavenumber.

3 Conclusions

On the basis of CCSD(T) calculations with the cc-pVQZ basis set and employing an empirical correction established earlier ([22] and references therein), accurate equilibrium structures have been obtained for linear C₁₃ and C₁₅. The ground-state rotational constant of the latter is estimated to be 92.2(1) MHz. This value should be of help to experimentalists in the analysis of forthcoming high-resolution spectroscopic investigations of this species. The IR active bending vibrations (π_u , symmetry) of C₁₃ and C₁₅ have been studied within the harmonic approximation which appears to work well for the fairly normal semi-rigid molecules. The *cis*-bending

**Fig. 4** CCSD(T)/cc-pVQZ wavenumbers of the lowest bending vibration of C_{2n+1} species

vibrations with highest wavenumber are predicted close to 500 cm⁻¹, ca. 300 cm⁻¹ below the results of previous SCF, CASSCF and B3LYP calculations with the cc-pVDZ basis for linear C₁₃ [16,17].

Figure 4 displays CCSD(T)/cc-pVQZ values for the lowest harmonic wavenumber of carbon chains of type C_{2n+1}. Again, C₃ provides the drastic exception while the results for the longer carbon chains show rather smooth behavior.

Throughout, calculated IR intensities for the *cis*-bending vibrations of linear C₁₃ and C₁₅ are smaller than 15 km mol⁻¹. For comparison, analogous calculations yield a large value of

2494 km mol⁻¹ for the ν_3 band of C₅ which has been observed in IRC+10216. On the basis of the present theoretical study, the chances to observe C₁₃ or C₁₅ through IR active bending vibrational transitions are considered to be poor.

Acknowledgements The author gratefully acknowledges friendship and collegiality with Prof. Hermann Stoll over a period of more than 30 years and wishes him the very best for the future. He thanks Profs. H.-J. Werner (University of Stuttgart) and P. J. Knowles (University of Cardiff) for continuously providing him with the latest version of MOLPRO. Financial support by the Fonds der Chemischen Industrie is gratefully acknowledged. The author wishes to thank Dr. R. Oswald for his help with the solution of a number of hardware and software problems in the course of the present work.

References

- Weltner W Jr, Van Zee RJ (1989) *Chem Rev* 89:1713
- van Orden A, Saykally RJ (1998) *Chem Rev* 98:2313
- Mladenović M, Schmatz S, Botschwina P (1994) *J Chem Phys* 101:5891 and references therein
- Hinkle KH, Keady JJ, Bernath PF (1988) *Science* 241:1319
- Cernicharo J, Goicoechea JR, Caux E (2000) *Astrophys J* 534:L199
- Giesen TF, van Orden AO, Cruzan JD, Provencal RA, Saykally RJ, Gendriesch R, Lewen F, Winnewisser G (2001) *Astrophys J* 551:L181; erratum (2001) *ibid* 555:L77
- Huggins W *Proc R Soc London*, 1881, 33:1; 1882, 34:148
- Jørgensen UG (1994) In: Jørgensen UG (ed.) *Molecules in the stellar environment*. Springer, Berlin Heidelberg New York
- Maier JP, Lakin NM, Walker GAH, Bohlender DA (2001) *Astrophys J* 553:267
- Oka T, Thorburn JA, McCall BJ, Friedman S, Hobbs LM, Sonnen-trucker P, Welty DE, York DG (2003) *Astrophys J* 582:823
- Cernicharo J, Goicoechea JR, Benilan Y (2003) *Astrophys J* 580:L157
- Bernath PF, Hinkle KH, Keady JJ (1989) *Science* 244:562
- Giesen TF, van Orden A, Hwang HJ, Fellers RS, Provencal RA, Saykally RJ (1994) *Science* 265:756
- Neubauer-Guenther P, Giesen TF, Berndt U, Fuch G, Winnewisser G (2002) *Spectrochim Acta A* 59:431
- Bleil R, Tao F-M, Kais S (1994) *Chem Phys Lett* 229:491
- Martin JML, Taylor PR (1995) *Chem Phys Lett* 240:521
- Martin JML, El-Yazal J, Francois J-P (1996) *Chem Phys Lett* 252:9
- Dunning TH Jr (1989) *J Chem Phys* 90:1007
- Botschwina P (2000) *Theor Chem Acc* 104:160
- Botschwina P (2002) *Chem Phys Lett* 354:148
- Botschwina P (2003) *Phys Chem Chem Phys (Invited Article)* 5:3337
- Botschwina P (2005) *Mol Phys* 103:1441
- Raghavachari K, Trucks GW, Pople JA, Head-Gordon M (1989) *Chem Phys Lett* 157:479
- Werner H-J, Knowles PJ (2003) with contributions from Amos RD, Bernhardsson A, Berning A, Celani P, Cooper DL, Deegan MJO, Dobbyn AJ, Eckert F, Hampel C, Hetzer G, Knowles PJ, Korona T, Lindh R, Lloyd AW, McNicholas SJ, Manby FR, Meyer W, Mura ME, Nicklass A, Palmieri P, Pitzer R, Rauhut G, Schütz M, Schumann U, Stoll H, Stone AJ, Tarroni R, Thorsteinsson T, MOLPRO, version 2002.6, a package of ab initio programs, see <http://www.molpro.net>
- Hampel C, Peterson K, Werner H-J (1992) *Chem Phys Lett* 190:1
- Deegan MJO, Knowles PJ (1994) *Chem Phys Lett* 227:321
- Heath JR, Saykally RJ (1991) *J Chem Phys* 94:1724
- Heath JR, Saykally RJ (1993) In: Reynolds JP (ed.) *On clusters and clustering, from atoms to fractals*. Elsevier Science Publishers BV, Amsterdam
- Botschwina P (2003) In: *Jahrbuch der Akademie der Wissenschaften zu Göttingen*, 2002, pp 272–279, Vandenhoeck and Ruprecht, Göttingen
- Kendall RA, Dunning TH Jr, Harrison RJ (1982) *J Chem Phys* 96:6796